

Physics 2102

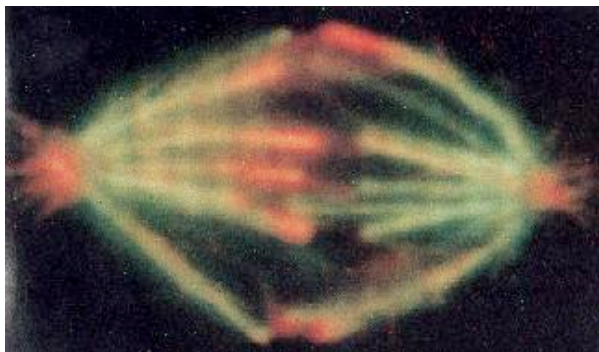
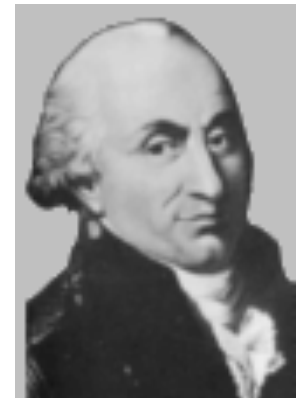
Christian Buth

# Physics 2102

## Lecture 4

### Electric Fields 2

Charles-Augustin  
de Coulomb  
(1736-1806)



Version: 01/21/2009

# Review 1

- New concept **field**: a physical property is associated with every point in space
- **Electric field**  $\vec{E} = \frac{\vec{F}}{q_0}$
- **Field lines** to visualize the direction and magnitude of an electric field
- Electric field of a point charge:  $E = kq/r^2$
- Electric field of a dipole:  $E \sim kp/r^3$

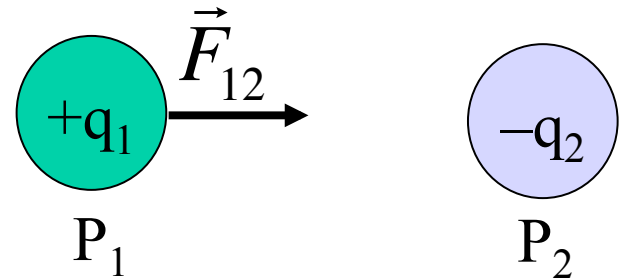
# Review 2

## Definition of Electric Field:

$$\vec{E} = \frac{\vec{F}}{q}$$

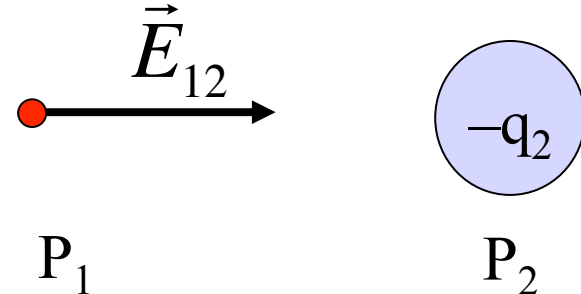
$$|\vec{F}_{12}| = \frac{k |q_1| |q_2|}{r_{12}^2}$$

E-Force  
on  
Charge



$$|\vec{E}_{12}| = \frac{k |q_2|}{r_{12}^2}$$

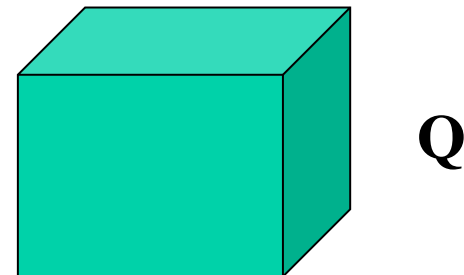
E-Field  
at Point



Units:  $F = [N] = [\text{Newton}]$  ;  $E = [N/C] = [\text{Newton/Coulomb}]$

# Continuous Charge Distribution

- Thus far, we have only dealt with **discrete, point charges**
- Imagine instead that a charge  $Q$  is smeared out over a:
  - Line
  - Area
  - Volume
- How to compute the electric field  $E$ ?



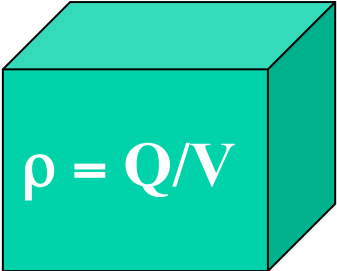
# Charge Density

- Useful idea: **charge density**
- Line of charge:  
charge per unit length =  $\lambda$
- Sheet of charge:  
charge per unit area =  $\sigma$
- Volume of charge:  
charge per unit volume =  $\rho$

$$\lambda = Q/L$$

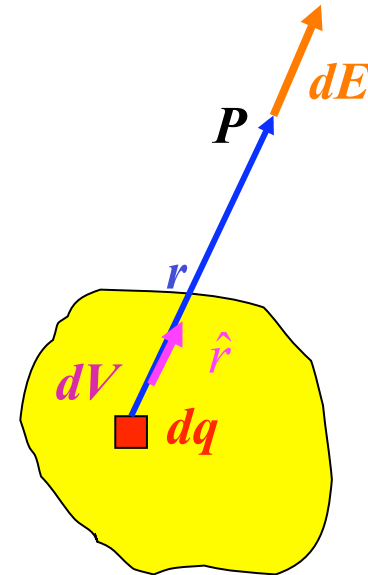
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$$\sigma = Q/A$$


$$\rho = Q/V$$

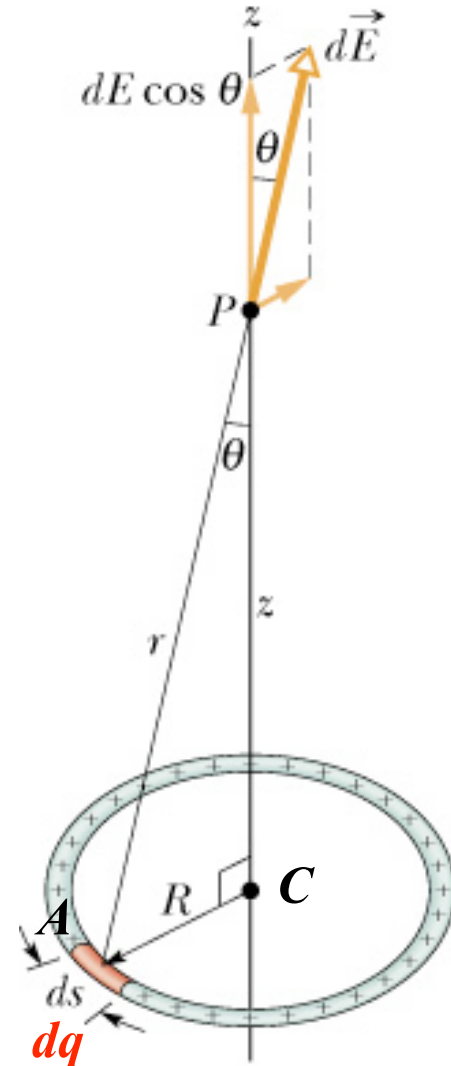
# Computing electric field of continuous charge distribution

- Approach: divide the continuous charge distribution into **infinitesimally small elements**
- Treat each element as a **point charge** and compute its electric field
- Sum (**integrate**) over all elements

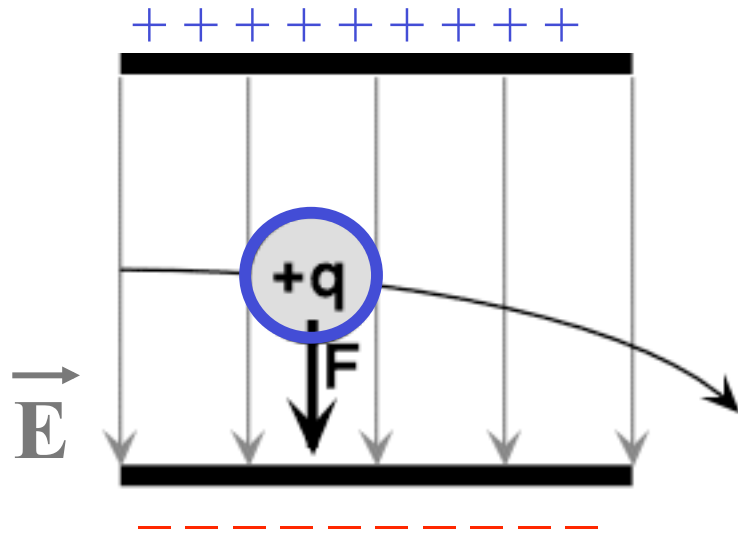


## Line of Charge

- **Uniform** line of charge, length  $L = 2\pi R$ , total charge  $Q$
- Compute explicitly the magnitude of  **$E$  at point P**
- The net field at P is in the **y direction** due to symmetry

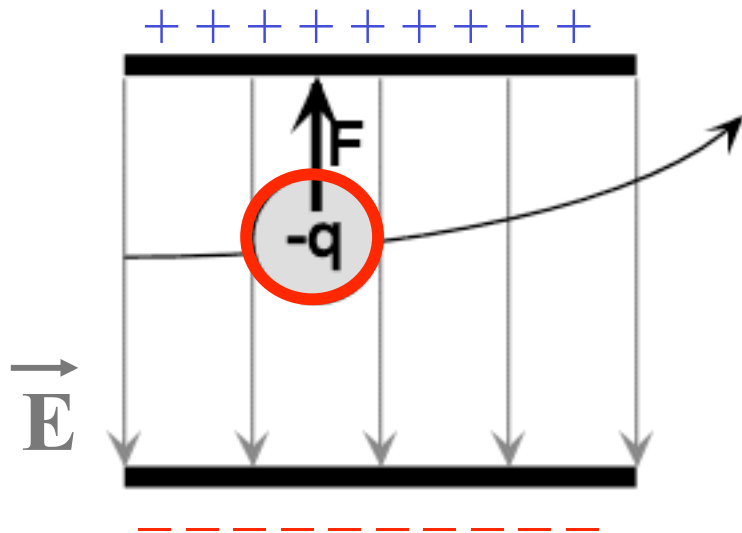


# Force on a Charge in Electric Field



Positive Charge  
Force in Same  
Direction as  $\vec{E}$ -Field

$$\vec{F} = q \vec{E}$$

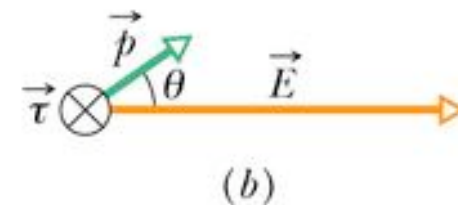
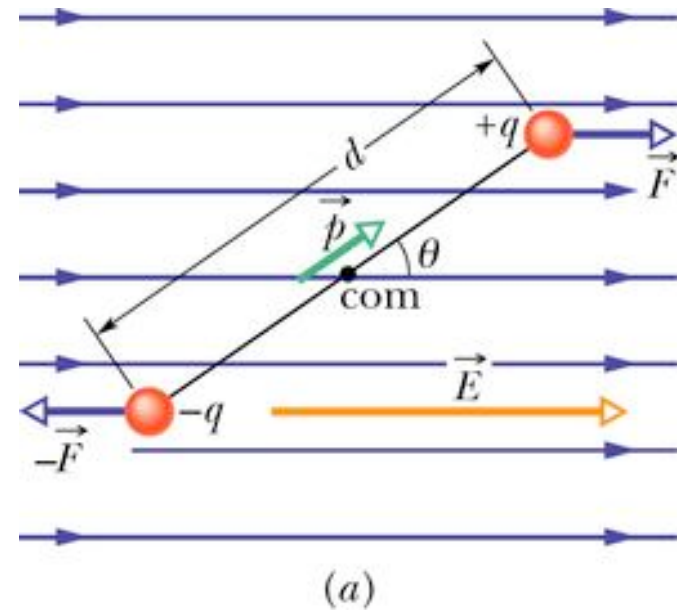


Negative Charge  
Force in Opposite  
Direction as  $\vec{E}$ -Field



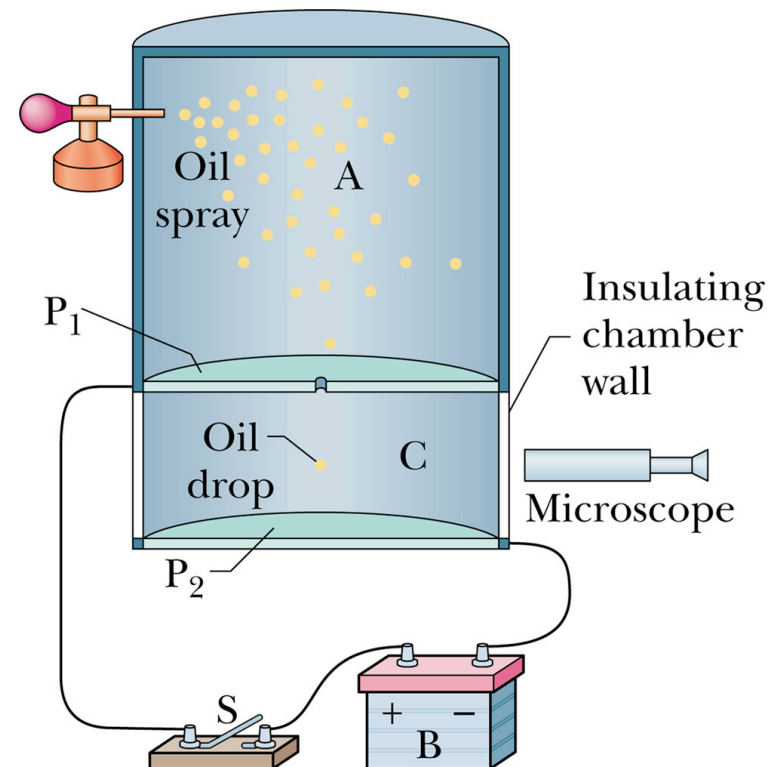
# Electric Dipole in a Uniform Field

- **Zero net force** on dipole; center of mass stays where it is
- Net **torque**: into page
- The dipole “aligns” itself with the field lines



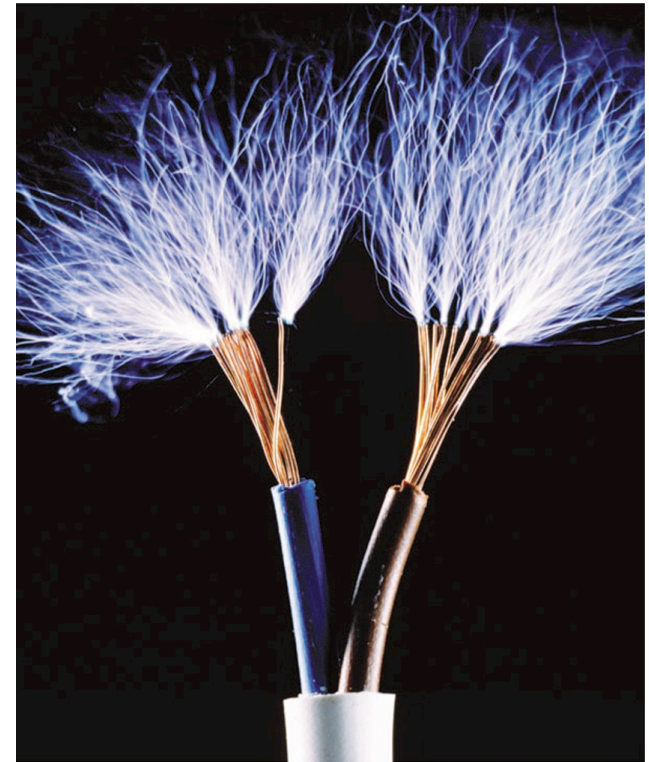
# Milliken experiment

- Charge is **quantized**, *i.e.*,  $q = n e$ ; measure the **elementary charge**  $e$
- **Downward** electric field in chamber C is switched on/off
- Negatively charged **oil droplets** drift upward/downward
- **Motion** allows one to determine the charge of droplets



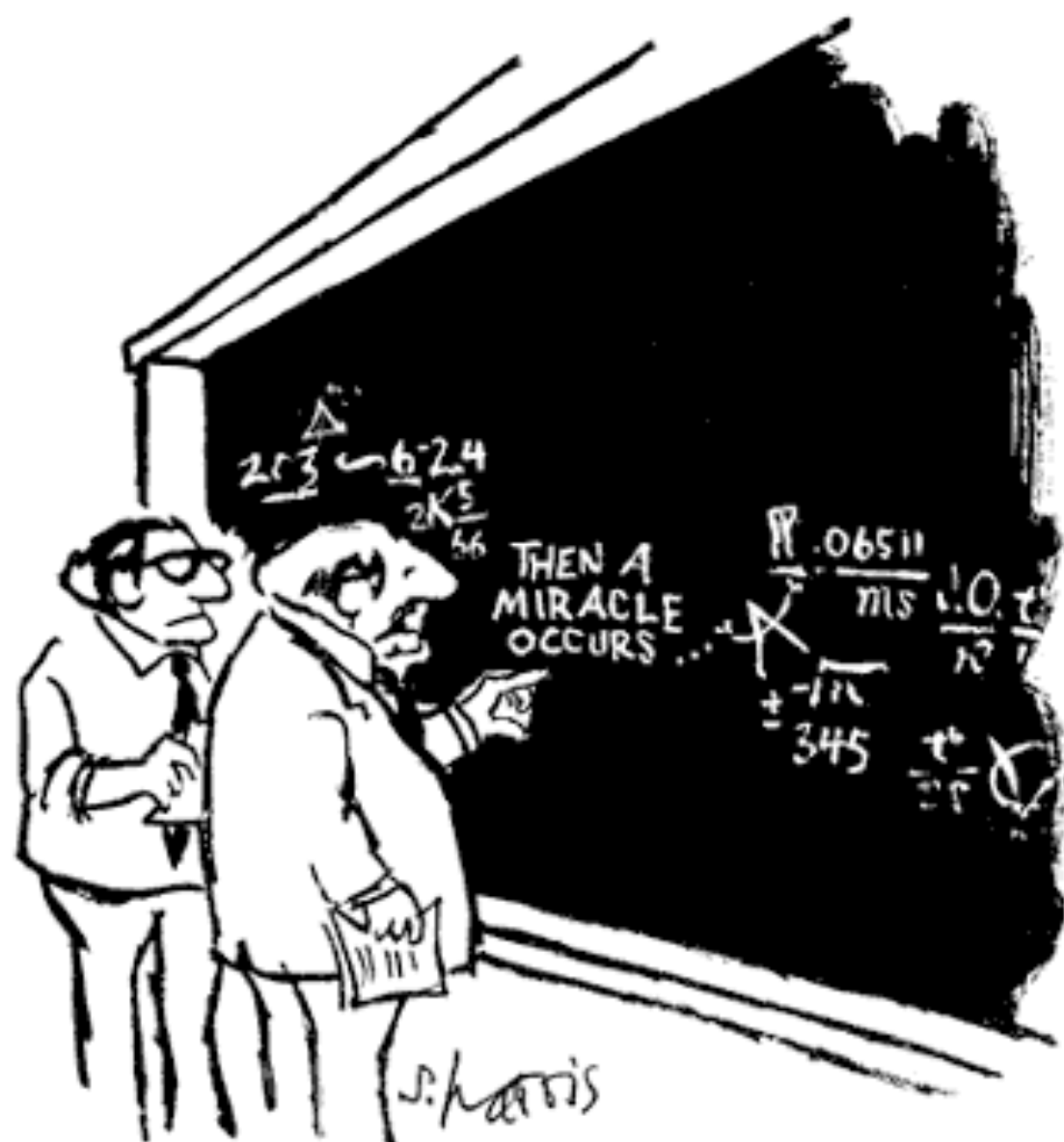
# Electrical Breakdown

- If electric field in air exceeds **critical value** then electrical breakdown occurs
- Electrons are **removed** from molecules in the air
- Electrons move in field and **collide** with other molecules which emit light
- **Air conducts**



# Summary

- **Continuous charge distributions** instead of discrete point charges
- Use **calculus** to find electric field from a continuous charge distribution
- For a **known** electric field, determine **force** on a charged particle via  $\vec{F} = q \vec{E}$
- Electric dipole **aligns along lines** of a uniform electric field
- **Milliken experiment** proves that charge is quantized; yields the magnitude of the **elementary charge**



"I think you should be more explicit here in step two."